

Principles of COMMUNICATIONS

Systems, Modulation, and Noise

SIXTH EDITION

INTERNATIONAL STUDENT VERSION



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